

# Information hiding: state-of-the-art and emerging trends

Quantified Information Flow

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# State-of-the-art

Two main quantitative techniques:

1-Information Theory: *How much information is leaked.*

2-Measuring bisimulation: *How bisimilar two systems are (e.g. DiPierro-Hankin-Wikickli).*

This talk will expand on Information Theory

# State-of-the-art

- How confidentiality is quantified using Information theory: Shannon's Mutual Information  $I(A;B)$  measure the dependency between r.v.  $A$  and  $B$
- $I(A;B/C)$  (conditional Mutual Information) measures the dependency between  $A$  and  $B$  given knowledge of  $C$
- $I(\text{Secret}; \text{Process} | \text{Public Input})$  = measure of the dependency between the process and the secret given knowledge of the public input = leakage

# How Information Theory works

- $P = \text{if } (h=0) \text{ access else deny,}$
- $h$  boolean var (uniform distribution). Then 1 bit is leaked:
- $P(h=0) \text{ Info}(\text{access}) + P(h=1) \text{ Info}(\text{deny}) =$   
 $\text{Entropy}(P) = I(h, P | \text{low}) = 0.5 \cdot 1 + 0.5 \cdot 1 = 1$
- Notice:  $P$  is not secure (motivation for quantitative analysis)

- *I(Secret;Process|Public Input)* pop out in different contexts to quantify interference (or related notions):
- Gray, Millen, (Abstract Machines)
- Clark-Hunt-Malacaria (Programming Languages),
- Boreale (Process Calculi)
- Chatzikokolakis-Palamidessi-Panangedan (Anonymity Protocols)

- The definition is supported by a "Non interference" theorem:
- $I(\text{Secret}; \text{Process} | \text{Public Input}) = 0$  **IFF** the system is "secure": proved by
- Millen (Abstract machines, 1987)
- Clark-Hunt-Malacaria (programming languages, 2002) ~ Classical non Interference
- Boreale (process algebra, 2006) ~ Abadi Gordon Secrecy

# Challenges

- How do we compute leakage in big real world programs?
- How do we integrate quantitative and qualitative security?
- How do we integrate quantitative and databases security (statistical inference)?
- Do quantitative bisimulation and Information Theory measure the same?