



## Foundational Results

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- Safety Question
- HRU Model
- Take-Grant Protection Model
- Expressive power
- Typed Access Matrix Model

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## What Is "Secure"?

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- Giving a generic right  $r$  to a subject who did not initially possess it is called "leaking"
- If a system  $S$ , beginning in initial state  $s_0$ , cannot leak right  $r$ , it is *safe* with respect to the right  $r$ .
- Leaking a right is not inherently bad
  - Legitimate transfer of rights by owner
- Safety Question
  - Does there exist an algorithm for determining whether a protection system  $S$  with initial state  $s_0$  is *safe* with respect to a generic right  $r$ ?

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## Formally:

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- Given
  - initial state  $X_0 = (S_0, O_0, A_0)$
  - Set of primitive commands  $c$
- Can we reach a state  $X_n$  ( $X_0 \vdash^* X_n$ ) where  $\exists s \in S$  and  $\exists o \in O$  such that  $A_n[s, o]$  includes a right  $r$  not in  $A_0[s, o]$ ?
  - If so, the system is not safe
  - But is a "safe" system a secure system?  
Are commands correctly implemented?

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## Trust

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- Safety does not distinguish a leak of a right from an authorized transfer of rights
  - Subjects authorized to receive transfer of rights deemed "trusted"
    - Eliminate trusted subjects from matrix
  - Trivial cases of safety
    - $r = read, own \in a[s, o]$ , command  $can \bullet grant \bullet read \bullet if \bullet own$
    - No command includes the *enter* primitive command
- How about the general case?

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## Mono-Operational Commands

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- Answer: *yes*
  - Sketch of proof:
    - Consider minimal sequence of commands  $c_1, \dots, c_k$  to leak the right.
    - Can omit **delete**, **destroy**
    - Can merge all **creates** into one (since new subjects are all equal)
- Worst case: insert every right into every entry; with  $s$  subjects and  $o$  objects initially, and  $n$  rights, upper bound is  $k \leq n(s+1)(o+1)$

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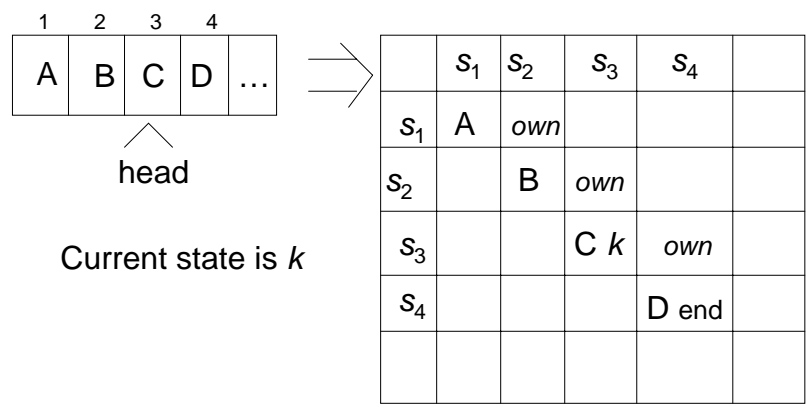
## General Case

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- Answer: *no*
- Sketch of proof:
  - Reduce halting problem to safety problem
  - Turing Machine review:
    - Infinite tape in one direction
    - States  $K$ , symbols  $M$ ; distinguished blank  $b$
    - Transition function  $\delta(k, m) = (k', m', L)$  means in state  $k$ , symbol  $m$  on tape location replaced by symbol  $m'$ , head moves to left one square, and enters state  $k'$
    - Halting state is  $q_{\hat{h}}$ ; TM halts when it enters this state

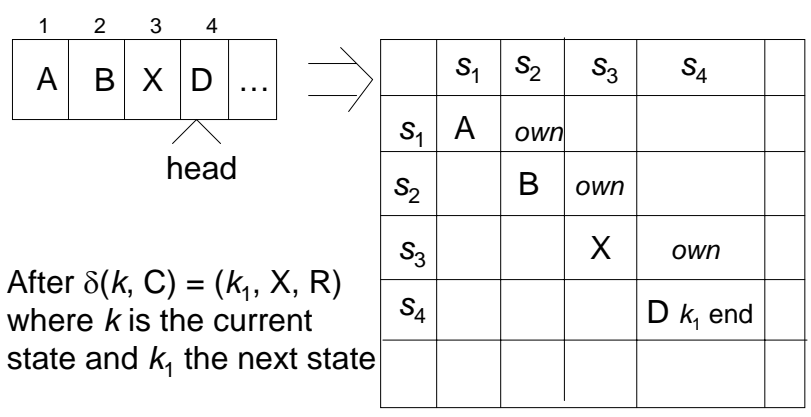
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# Mapping



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# Mapping



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## Command Mapping

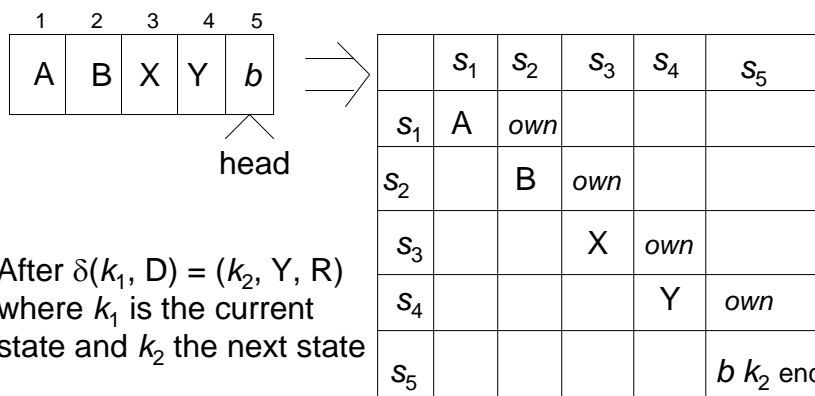
$\delta(k, C) = (k_1, X, R)$  at intermediate becomes

```

command  $c_{k,C}(s_3, s_4)$ 
if own in  $A[s_3, s_4]$  and  $k$  in  $A[s_3, s_3]$ 
    and  $C$  in  $A[s_3, s_3]$ 
then
    delete  $k$  from  $A[s_3, s_3]$ ;
    delete  $C$  from  $A[s_3, s_3]$ ;
    enter  $X$  into  $A[s_3, s_3]$ ;
    enter  $k_1$  into  $A[s_4, s_4]$ ;
end
  
```

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## Mapping



After  $\delta(k_1, D) = (k_2, Y, R)$   
 where  $k_1$  is the current  
 state and  $k_2$  the next state

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## Command Mapping

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$\delta(k_1, D) = (k_2, Y, R)$  at end becomes

```
command crightmostk,c(s4, s5)
if end in A[s4, s4] and k1 in A[s4, s4]
    and D in A[s4, s4]
then
    delete end from A[s4, s4];
    create subject s5;
    enter own into A[s4, s5];
    enter end into A[s5, s5];
    delete k1 from A[s4, s4];
    delete D from A[s4, s4];
    enter Y into A[s4, s4];
    enter k2 into A[s5, s5];
end
```

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## Rest of Proof

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- Protection system exactly simulates a TM
  - Exactly 1 *end* right in ACM
  - 1 right in entries corresponds to state
  - Thus, at most 1 applicable command
- If TM enters state  $q_f$  then right has leaked
- If safety question decidable, then represent TM as above and determine if  $q_f$  leaks
  - Implies halting problem decidable
- Conclusion: safety question undecidable

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## Other Results

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- Set of unsafe systems is recursively enumerable
- Delete **create** primitive; then safety question is complete in **P-SPACE**
- Delete **destroy, delete** primitives (this system is called monotonic): safety question is undecidable
- Safety question for monoconditional, monotonic protection systems is decidable
- Safety question for monoconditional protection systems with **create, enter, delete** (and no **destroy**) is decidable.

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## Where does this leave us?

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- Safety decidable for some models
  - Are they practical?
- Safety only works if maximum rights known in advance
  - Policy must specify all rights someone could get, not just what they have
- Can the safety of a particular system, with specific rules, be established?

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## Take-Grant Protection Model

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- A specific (not generic) system
  - System represented as a directed graph
  - Set of graph rewriting rules for state transitions
- Safety is decidable, and in time linear with the size of the system
- Goal: find conditions under which rights can be transferred from one entity to another in the system

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## System

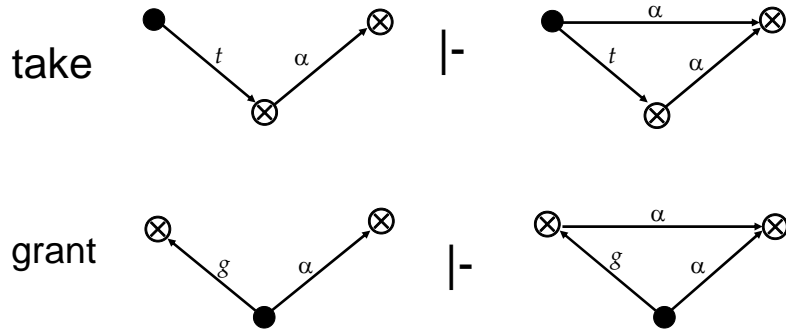
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- objects (files, ...)
- subjects (users, processes, ...)
- ⊗ don't care (either a subject or an object)
- $G \mid -_x G'$  apply a rewriting rule  $x$  (witness) to  $G$  to get  $G'$
- $G \mid -^* G'$  apply a sequence of rewriting rules (witness) to  $G$  to get  $G'$
- $R = \{ t, g, r, w, \dots \}$  set of rights

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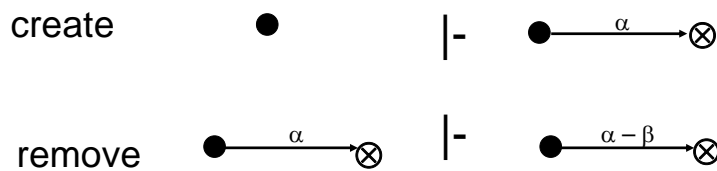


## Rules



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## More Rules



These four rules are called the *de jure* rules

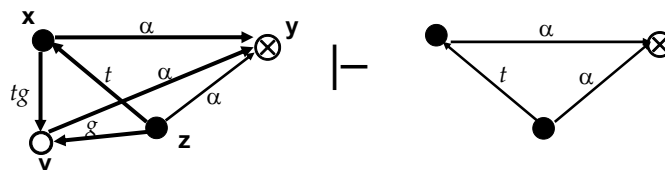
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## Example: Shared Buffer

- Initially  $s$  has grant rights for processes  $p$  and  $q$ .
- $s$  sets up a shared buffer for  $p, q$  with the following steps
  - $s$  creates new object  $b$
  - $s$  grants  $(\{r, w\}$  to  $b)$  to  $p$
  - $s$  grants  $(\{r, w\}$  to  $b)$  to  $q$

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## Symmetry



1.  $x$  creates ( $tg$  to new)  $v$
  2.  $z$  takes ( $g$  to  $v$ ) from  $x$
  3.  $z$  grants ( $\alpha$  to  $y$ ) to  $v$
  4.  $x$  takes ( $\alpha$  to  $y$ ) from  $v$
- Similar result for grant

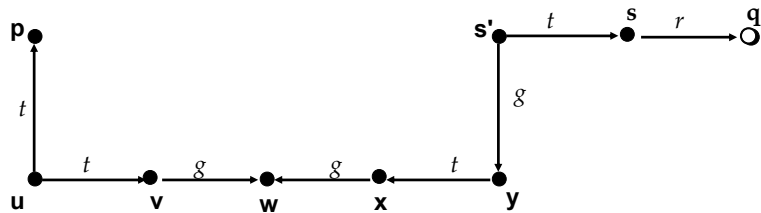
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## Islands

- $tg$ -path: path of distinct vertices connected by edges labeled  $t$  or  $g$ 
  - Call them "tg-connected"
- island: maximal  $tg$ -connected subject-only subgraph
  - Any right one vertex has can be shared with any other vertex

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## Example



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## can•share Predicate

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Definition:

$\text{can}\bullet\text{share}(r, \mathbf{x}, \mathbf{y}, G_0)$  if, and only if, there is a sequence of protection graphs  $G_0, \dots, G_n$  such that  $G_0 \dashv^* G_n$  using only *de jure* rules and in  $G_n$  there is an edge from  $\mathbf{x}$  to  $\mathbf{y}$  labeled  $r$ .

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## can•share Properties

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- If  $\mathbf{x}$  and  $\mathbf{y}$  are subjects in an island, then  $\text{can}\bullet\text{share}(r, \mathbf{x}, \mathbf{y}, G_0)$ 
  - Proof by induction using the properties of tg-connected subjects
- General result:  $\text{can}\bullet\text{share}(r, \mathbf{x}, \mathbf{y}, G_0)$  is decidable using an algorithm of complexity  $O(|V| + |E|)$  where  $V$  and  $E$  are the vertices and edges in the graph
  - Proof omitted (Exercise)

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## Key Question

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- Characterize class of models for which safety is decidable
  - Existence: Take-Grant Protection Model is a member of such a class
  - Universality: in general, the question undecidable, so for some models it is not decidable
- What is the dividing line?

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## Typed Access Matrix Model

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- Like ACM, but with set of types  $T$ 
  - All subjects, objects have types
  - Set of types for subjects  $TS$
- Protection state is  $(S, O, \tau, A)$ 
  - $\tau: O \rightarrow T$  specifies type of each object
  - If  $X$  subject,  $\tau(X)$  in  $TS$
  - If  $X$  object,  $\tau(X)$  in  $T - TS$
- Same rules as ACM except for create

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## Create Rules

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- Subject creation
  - **create subject  $s$  of type  $ts$**
  - $s$  must not exist as subject or object when operation executed
  - $ts \in TS$
- Object creation
  - **create object  $o$  of type  $to$**
  - $o$  must not exist as object when operation executed
  - $to \in T - TS$

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## Create Subject

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- Precondition:  $s \notin S$
- Primitive command: **create subject  $s$  of type  $t$**
- Postconditions:
  - $S' = S \cup \{s\}, O' = O \cup \{s\}$
  - $(\forall y \in O)[\tau'(y) = \tau(y)], \tau'(s) = t$
  - $(\forall y \in O')[a'[s, y] = \emptyset], (\forall x \in S')[a'[x, s] = \emptyset]$
  - $(\forall x \in S)(\forall y \in O)[a'[x, y] = a[x, y]]$

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## Create Object

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- Precondition:  $o \notin O$
- Primitive command: **create object  $o$  of type  $t$**
- Postconditions:
  - $S' = S, O' = O \cup \{o\}$
  - $(\forall y \in O)[\tau'(y) = \tau(y)], \tau'(o) = t$
  - $(\forall x \in S')[a'[x, o] = \emptyset]$
  - $(\forall x \in S)(\forall y \in O)[a'[x, y] = a[x, y]]$

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## Definitions

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- MTAM (Monotonic TAM ) Model: TAM model without **delete, destroy**
- $\alpha(x_1:t_1, \dots, x_n:t_n)$  create command
  - $t_i$  child type in  $\alpha$  if any of **create subject  $x_j$  of type  $t_j$**  or **create object  $x_j$  of type  $t_j$**  occur in body of  $\alpha$
  - $t_i$  parent type otherwise

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## Cyclic Creates

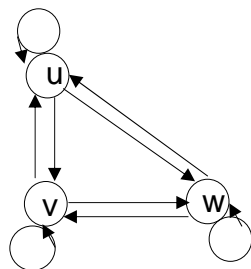
```
command havoc( $s_1 : u, s_2 : u, o_1 : v, o_2 : v, o_3 : w, o_4 : w$ )  
  create subject  $s_1$  of type  $u$ ;  
  create object  $o_1$  of type  $v$ ;  
  create object  $o_3$  of type  $w$ ;  
  enter  $r$  into  $a[s_2, s_1]$ ;  
  enter  $r$  into  $a[s_2, o_2]$ ;  
  enter  $r$  into  $a[s_2, o_4]$ ;
```

End

What kind of types are  $u, v$  and  $w$ ?

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## Creation Graph



- $u, v, w$  child types
- $u, v, w$  also parent types
- Graph: lines from parent types to child types
- This graph has cycles

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## Theorems

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- Safety decidable for systems with acyclic MTAM schemes
- Safety for acyclic ternary MATM decidable in time polynomial in the size of the initial ACM
  - “ternary” means commands have no more than 3 parameters
  - Equivalent in expressive power to MTAM

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## Key Points

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- Safety problem undecidable
- Limiting scope of systems can make problem decidable
- Types critical to safety problem’s analysis

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