



## Access Control Matrix

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- Protection state of system
  - Part of the system state (contents of memory locations, registers, etc.)
  - Describes current settings, values of system relevant to protection
- Access control matrix
  - Describes protection state precisely
  - Matrix describing rights of subjects
  - State transitions change elements of matrix

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## Protection state

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- State transitions change the system and therefore the protection state
- From all the states P of system, only those in Q considered safe (acceptable)
- **Security Policy** characterizes the states in Q
- **Security Mechanisms** prevent system from entering states in P-Q

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## Access Control Matrix

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- Used to indicate **who** is allowed to do **what** to/with **whom** on the system.
- Who is **who** ?
  - **Subject** is what we call active entities (processes, users, other computers) that want to “do something”
- The **what** the subject does with the object can be just about anything, and it may be multi-part.
  - The set of rights in a cell specify the access of the subject (row) to the object (column)
  - Typical manipulations include
    - READ, MODIFY, CREATE, CHANGE, DELETE

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## Object

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- **Object** is what we call the broad category of items which can be manipulated or accessed
- Usually objects are passive, for example:
  - File
  - Directory (or Folder)
  - Memory segment
- An entity might be considered a **subject** in some circumstances but in other ones be an **object** on which it is possible to perform operations such as
  - kill
  - suspend
  - resume

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## Operations can require multiple access rights

- Example: User *parisi* (subject) wishes to copy (manipulate) the file */etc/passwd* (object1) to his home *directory* (object2)
- On many systems it requires access checks as in the following:
  - *parisi* needs permission to read OBJECT1
  - *parisi* needs permission to create a new file (OBJECT3) in OBJECT2
  - *parisi* needs permission to append to (or write to) OBJECT3

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## Description of ACM

		objects (entities)					
		$o_1$	...	$o_m$	$s_1$	...	$s_n$
subjects	$s_1$						
	$s_2$						
	...						
	...						
	$s_n$						

- Subjects  $S = \{ s_1, \dots, s_n \}$
- Objects  $O = \{ o_1, \dots, o_m \}$
- Rights  $R = \{ r_1, \dots, r_k \}$
- Entries  $A[s_i, o_j] \subseteq R$
- $A[s_i, o_j] = \{ r_{x'}, \dots, r_y \}$  means subject  $s_i$  has rights  $r_{x'}, \dots, r_y$  over object  $o_j$

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## Example 1

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- Processes  $p, q$
- Files  $f, g$
- Rights  $r, w, x, a, o$

	$f$	$g$	$p$	$q$
$p$	$rwo$	$r$	$rwXO$	$w$
$q$	$a$	$ro$	$r$	$rwXO$

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## Example 2

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- Procedures (subjects)  $inc\_ctr, dec\_ctr, manage$
- Variable (object)  $counter$
- Rights  $+, -, call$

	$counter$	$inc\_ctr$	$dec\_ctr$	$manage$
$inc\_ctr$	$+$			
$dec\_ctr$	$-$			
$manage$		$call$	$call$	$call$

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## State Transitions

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- Change the protection state of system
- $|-$  represents transition
  - $X_i |-\tau X_{i+1}$ : command  $\tau$  moves system from state  $X_i$  to  $X_{i+1}$
  - $X_i |-\ast Y$ : a sequence of commands moves system from state  $X_i$  to  $Y$
- Commands often called *transformation procedures*

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## Primitive Operations

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- **create subject  $s$ ; create object  $o$** 
  - Creates new row, column in ACM; creates new column in ACM
- **destroy subject  $s$ ; destroy object  $o$** 
  - Deletes row, column from ACM; deletes column from ACM
- **enter  $r$  into  $A[s, o]$** 
  - Adds  $r$  rights for subject  $s$  over object  $o$
- **delete  $r$  from  $A[s, o]$** 
  - Removes  $r$  rights from subject  $s$  over object  $o$

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## Create Subject

- Precondition:  $s \notin S$
- Primitive command: **create subject  $s$**
- Postconditions:
  - $S' = S \cup \{s\}, O' = O \cup \{s\}$
  - $(\forall y \in O')[a[s, y] = \emptyset],$
  - $(\forall x \in S')[a[x, s] = \emptyset]$
  - $(\forall x \in S)(\forall y \in O)[a[x, y] = a[x, y]]$

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## Create Subject

- Precondition:  $s \notin S$
- Primitive command: **create subject  $s$**

	p	q
x	$r_1$	$r_1, r_2$
y		$r_1$

→

	p	q
x	$r_1$	$r_1, r_2$
y		$r_1$
s		

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## Create Object

- Precondition:  $o \notin O$
- Primitive command: **create object  $o$**
- Postconditions:
  - $S' = S, O = O \cup \{o\}$
  - $(\forall x \in S')[a[x, o] = \emptyset]$
  - $(\forall x \in S)(\forall y \in O)[a[x, y] = a[x, y]]$

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## Create Object

- Precondition:  $o \notin O$
- Primitive command: **create object  $o$**

	p	q
x	$r_1$	$r_1, r_2$
y		$r_1$

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	p	q	o
x	$r_1$	$r_1, r_2$	
y		$r_1$	

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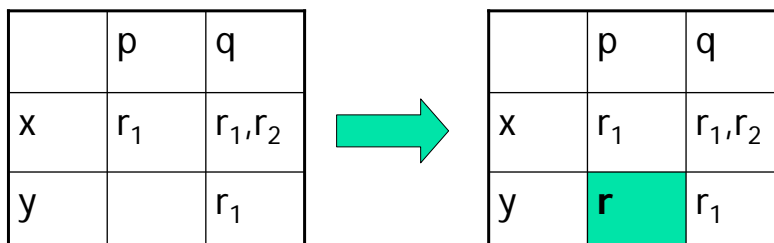
## Add Right

- Precondition:  $s \in S, o \in O$
- Primitive command: enter  $r$  into  $a[s, o]$
- Postconditions:
  - $S' = S, O' = O$
  - $a'[s, o] = a[s, o] \cup \{r\}$
  - $(\forall x \in S')(\forall y \in O' - \{o\}) [a'[x, y] = a[x, y]]$
  - $(\forall x \in S' - \{s\})(\forall y \in O') [a'[x, y] = a[x, y]]$

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## Add Right

- Precondition:  $p \in S, y \in O$
- Primitive command: **enter  $r$  into  $a[p, y]$**



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## Delete Right

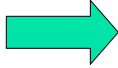
- Precondition:  $s \in S, o \in O$
- Primitive command: **delete**  $r$  from  $a[s, o]$
- Postconditions:
  - $S' = S, O' = O$
  - $a'[s, o] = a[s, o] - \{ r \}$
  - $(\forall x \in S')(\forall y \in O' - \{ o \}) [a'[x, y] = a[x, y]]$
  - $(\forall x \in S' - \{ s \})(\forall y \in O') [a'[x, y] = a[x, y]]$

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## Delete Right

- Precondition:  $p \in S, y \in O$
- Primitive command: **delete**  $r$  from  $a[p, y]$

	p	q
x	$r_1$	$r_1, r_2$
y	r	$r_1$



	p	q
x	$r_1$	$r_1, r_2$
y		$r_1$

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## Destroy Subject

- Precondition:  $s \in S$
- Primitive command: **destroy subject  $s$**
- Postconditions:
  - $S' = S - \{s\}, O' = O - \{s\}$
  - ~~$(\forall y \in O')[a'[s, y] = \emptyset],$~~
  - ~~$(\forall x \in S')[a'[x, s] = \emptyset]$~~
  - $(\forall x \in S')(\forall y \in O') [a'[x, y] = a[x, y]]$

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## Destroy Subject

- Precondition:  $s \in S$
- Primitive command: **destroy subject  $s$**

	p	q
x	$r_1$	$r_1$
y		$r_1$
s	$r_2$	



	p	q
x	$r_1$	$r_1, r_2$
y		$r_1$

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## Destroy Object

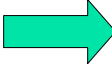
- Precondition:  $o \in O$
- Primitive command: **destroy object**  $o$
- Postconditions:
  - $S' = S, O' = O - \{o\}$
  - ~~$(\forall x \in S')[a[x, o] = \emptyset]$~~
  - $(\forall x \in S')(\forall y \in O) [a[x, y] = a[x, y]]$

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## Destroy Object

- Precondition:  $o \in O$
- Primitive command: **destroy object**  $o$

	p	q	<b>o</b>
x	r <sub>1</sub>	r <sub>1</sub> ,r <sub>2</sub>	r <sub>2</sub>
y		r <sub>1</sub>	



	p	q
x	r <sub>1</sub>	r <sub>1</sub> ,r <sub>2</sub>
y		r <sub>1</sub>

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## Creating File

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- Process  $p$  creates file  $f$  with  $r$  and  $w$  permission

```
command create_file( $p$ ,  $f$ )
  create object  $f$ ;
  enter own into  $A[p, f]$ ;
  enter  $r$  into  $A[p, f]$ ;
  enter  $w$  into  $A[p, f]$ ;
end
```

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## Mono-Operational Commands

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- Make process  $p$  the owner of file  $g$

```
command make_owner( $p$ ,  $g$ )
  enter own into  $A[p, g]$ ;
end
```

- Mono-operational command
  - Single primitive operation in this command

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## Conditional Commands

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- Let  $p$  give  $q$   $r$  rights over  $f$ , if  $p$  owns  $f$

```
command grant_read_file_1(p, f, q)
  if own in  $\bar{A}[p, f]$ 
  then
    enter  $r$  into  $A[q, f]$ ;
  end
```

- Mono-conditional command
  - Single condition in this command

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## Multiple Conditions

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- Let  $p$  give  $q$  the rights  $r$  and  $w$  over  $f$ , if  $p$  owns  $f$  and  $p$  has  $c$  rights over  $q$

```
command grant_read_file_2(p, f, q)
  if own in  $\bar{A}[p, f]$  and  $c$  in  $A[p, q]$ 
  then
    enter  $r$  into  $A[q, f]$ ;
    enter  $w$  into  $A[q, f]$ ;
  end
```

NOTE: `or` and `not` are not allowed in conditions.

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## Copy Right

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- Allows possessor to give rights to another (sometimes called grant right)
- Copier may or may not surrender the right, depending on system
- Often attached to a right, so only applies to that right
  - $r$  is read right that cannot be copied
  - $rc$  is read right that can be copied
- Is copy flag copied when giving  $r$  rights?
  - Depends on model, instantiation of model

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## Own Right

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- Usually allows possessor to change entries in ACM column
  - So owner of object can add, delete rights for others
  - May depend on what system allows
    - Cannot give rights to specific (set of) users
    - Cannot pass copy flag to specific (set of) users

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## Attenuation of Privilege

- Principle says you cannot give rights you do not possess
  - Restricts addition of rights within a system
  - Usually *ignored* for owner
    - Why? Owner gives herself rights, gives them to others, deletes her rights.

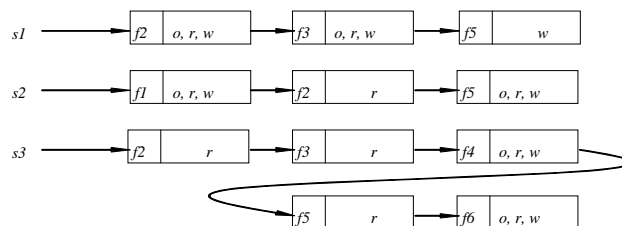
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## ACM implementation 1

o: own  
r: read  
w: write

	f1	f2	f3	f4	f5	f6
s1		a, r, w	a, r, w		w	
s2	a, r, w	r			a, r, w	
s3		r	r	a, r, w	r	a, r, w

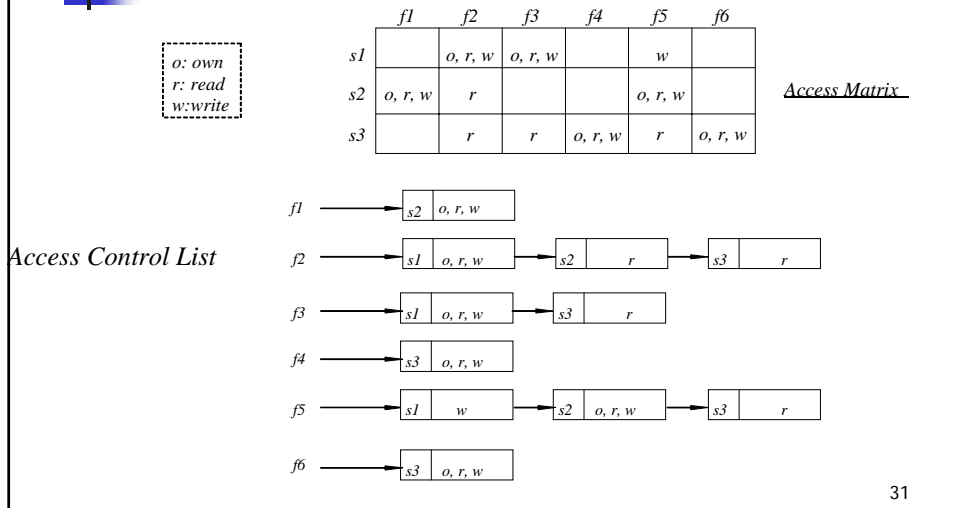
*Access Matrix*



*Capabilities*

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## ACM implementation 2



## Key Points

- Access control matrix simplest abstraction mechanism for representing protection state
- Transitions alter protection state
- 6 primitive operations alter matrix
  - Transitions can be expressed as commands composed of these operations and, possibly, conditions

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