

# Routing in Outer Space: Fair Traffic Load in Multi-Hop Wireless Networks\*

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## ABSTRACT

In this paper we consider security-related and energy-efficiency issues in multi-hop wireless networks. We start our work from the observation, known in the literature, that shortest path routing creates congested areas in multi-hop wireless networks. These areas are critical—they generate both security and energy efficiency issues. We attack these problems and set out routing in outer space, a new routing mechanism that transforms any shortest path routing protocol (or approximated versions of it) into a new protocol that does not create congested areas, does not have the associated security-related issues, and does not encourage selfish positioning. Moreover, the network lives longer of the same network using the original routing protocol (in spite of using more energy globally), and dies more gracefully.

## Categories and Subject Descriptors

C.2.1 [Computer-Communications Networks]: Network Architecture and Design—*Distributed networks, Network communications, Wireless Communication*; C.2.2 [Computer-Communications Networks]: Network Protocols—*Routing Protocols*

## General Terms

Performance, security,

## Keywords

Multi-hop wireless networks, analysis, energy-efficiency, routing, load-balancing, simulations.

## 1. INTRODUCTION

During the past years the interest in multi-hop wireless networks has been growing significantly. These networks have an important

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functionality that is the possibility to use other nodes as relays in order to deliver messages and data from sources to destinations. This functionality makes multi-hop wireless networks not only scalable but also usable in various areas and contexts. One of the most representative and important examples of multi-hop wireless networks are wireless sensor networks where small devices equipped with a radio transmitter and a battery are deployed in a geographic area for monitoring or measuring of some desired property like temperature, pressure, or others [1, 18].

Routing in a wireless sensor network is one of the most interesting and difficult issues to solve due to the limited resources and capacities of the nodes. Protocols that use less information possible and need minimal energy consumption of nodes have become more than valuable in this context. Much research work has been devoted to finding energy-efficient routing protocols for this kind of networks. Often, these protocols tend to find an approximation of the shortest path between the source and the destination of the message. In [17], the authors analyze the impact of shortest path routing in a large multi-hop wireless network. They show that relay traffic induces congested areas in the network. If the traffic pattern is uniform, i. e. every message has a random source and a random destination uniformly and independently chosen, and the network area is a disk, then the center of the disk is a congested area, where the nodes have to relay much more messages than the other nodes of the network.

We have the same problem if the network area is a square, or a rectangle, or any other two-dimensional convex surface. Our experiments show that, when using geographic routing [15] on a network deployed in a square, 25% of the messages are relayed by the nodes in a small central congested region whose area is 3% of the total area of the square.

Congested areas are bad for a number of important reasons. They raise security-related issues: If a large number of messages are relayed by the nodes deployed in a relatively small congested region, then jamming can be a vicious attack. It is usually expensive to jam a large geographical area, it is much cheaper and effective to jam a small congested region. In the square, for example, it is enough to jam 3% of the network area to stop 25% of the messages. Moreover, if an attacker has the goal of getting control over as many communications as possible, then it is enough to control 3% of the network nodes to handle 25% of the messages.

There are also energy-efficiency issues: Aside from re-transmissions, that are costly and, in congested areas, more frequent, the nodes have to relay a much larger number of messages. Therefore the nodes in these areas will die earlier than the other nodes in the network, exacerbating the problem for the nodes in the same area that are still operational. In the long run, this results in holes in the network and in a faster, and less graceful, death of the sys-

tem. Note that these problems are not solved by trying to balance the load just locally, as done by a few protocols in the literature (like GEAR [35], for example)—these protocols are useful, they can be used in any case (in our protocols as well), and are efficient in smoothing the energy requirements among neighbors, while they can’t do much against congested areas and they don’t help to alleviate the above discussed security-related issues.

Lastly, there may be other concerns in the contexts where the nodes are carried by individual independent entities. In this paper we do not consider mobility. However, if the position of the node can be chosen by the node in such a way to maximize its own advantage, and if energy is an issue, then every node would stay close to the border, where it can get the same services without having to relay other nodes’ messages. If the nodes are selfish, an uneven distribution of the load in the network area leads to an irregular distribution of the nodes—there is no point in positioning in the place where the battery is going to last the shortest. Selfish behavior is a recent concern in the networking community and it is rapidly gaining importance [15, 30, 31]. These mechanisms can be used to force selfish nodes to execute truthfully the protocol, wherever they are positioned, but they do not help in preventing selfish positioning or moving. For the best of our knowledge, here we are raising a new concern, that can be important in mobile networks or whenever the position of the node can be an independent and selfish choice, like in networks of individuals (e. g. students in a university campus network).

Solving these issues—security, energy-efficiency, and tolerance to (a particular case of) selfish behavior—is an important and non-trivial problem, and, at least partially, our goal. In this paper we attack this problem and set out *routing in outer space*, a new routing mechanism that transforms any shortest path routing protocol (or approximated versions of it) into a new protocol that, in case of uniform traffic, guarantees that the network does not have congested areas, does not have the associated security issues, and, in spite of using more energy globally, lives longer of the same network using the original routing protocol—that is, it is more energy-efficient. We support our claims by showing routing in outer space based on geographic routing, and by performing a large set of experiments.

The rest of the paper is organized as follows: In Section 2 we report on the relevant literature in this area; in Section 3 we present the theoretical idea behind our work, we come up with routing in outer space, and prove its mathematical properties; in Section 4, after describing our node and network assumptions and our simulation environment, we discuss on the practical issues related to implementing routing in outer space starting from geographic routing; lastly, we present an extensive set of experiments, fully supporting our claims.

## 2. RELATED WORK

Routing in multi-hop wireless networks is one of most important, interesting, and challenging problems due to network devices limitations and network dynamics. As a matter of fact this is one of the most studied topics in this area, and the literature on routing protocols for multi-hop wireless networks is vast. There have been proposed protocols that maintain routes continuously (based on distance vector) [21, 36, 27], that create routes on-demand [14, 19, 20], or a hybrid [9]. For a good survey and comparison see [4, 26]. Other examples of routing protocols for multi-hop wireless networks are those based on link-state like OLSR [13], and others.

Geographic routing or position-based routing, where nodes locally decide the next relay on the basis based on information obtained through some GPS (Global Positioning System) or other lo-

cation determination techniques [10], seems to be one of the most feasible and studied approach. Examples of research work on this approach are protocols like GEAR [35] and GAF [34]. For a good starting survey see [29].

All these protocols try to approximate the shortest path between source and destination over the network. In [22], the authors analytically study the impact of shortest single-path routing on node traffic load by approximating single paths to line segments, and show that multi-path routing, although introducing a larger overhead, provides better congestion and traffic balancing. Further work in the same direction [7] shows that multi-path routing can balance load only if a very high number of paths is used. In [17], the authors analyze the load for a homogeneous multi-hop wireless network for the case of straight line routing. Assuming uniform traffic, it is proven that relays induce so called hotspots or congested areas in the network. Of course, geographic routing (which, in dense networks, approximates the shortest path between source and destination) also suffers of the same problems.

The problem of reducing congestion on the center of a network deployed in a disk in the case of uniform traffic has been considered in [12]. The authors consider a number of possible heuristics like selecting routes along inner and outer radii and switching between them at a random point, moving between the radii linearly, and so on. Later, in [23], the same issues are addressed. In this work the authors present a theoretical approach to solve the problem showing that an optimum routing scheme based on shortest paths can be expressed in terms of geometric optics and computed by linear programming. Being the optimal trajectories they find not expressible by closed form formulas, hence not applicable in practice, they also present a practical solution that approximates the optimum. This solution is shown to be implementable and close to the optimum in the case of the disk, while its performance is not as good in the case of the square. In particular, routing in outer space has a better reported decrease of the central load, and provides other interesting properties, like independence of the load of the node’s position.

A lot of work has been done regarding energy-efficiency issues, and several approaches try to solve the problem locally, like [35, 39]. These approaches are useful to balance the load reactively and to smooth the energy level among neighbors, while they cannot remove congested areas. These solutions can be used in routing in outer space as well to get locally a smoother load among neighbors.

## 3. ROUTING IN OUTER SPACE

We model the multi-hop wireless network as a undirected graph  $G = (V, E)$ , where  $V$  is the set of nodes and  $E$  is the set of edges. The nodes are ad-hoc deployed on the network area  $S$ . Formally, it is enough to assume that  $S$  is a metric space with distance  $d_S$  and that every node is a point on  $S$ . Given two nodes  $u, v \in V$  deployed on  $S$ , we will denote the distance between their positions on the space with  $d_S(u, v)$ . The nodes have a transmission range  $r$ —two nodes  $u, v \in V$  are connected by a wireless link  $uv \in E$  if  $d_S(u, v) \leq r$ , that is, their distance is at most  $r$ . The common practice in the literature is to take a convex surface as  $S$ , usually a square, a rectangle, or a disk, with the usual Euclidean distance. In this paper we assume that the nodes know their position, either by being equipped with a GPS unit or by using one of the many localization protocols [5, 28], and that they know the boundaries of the network area  $S$ ; this is possible either by pre-loading this information on the nodes before deployment, or by using one of the protocols in [6, 16, 32].

We started from the observation that shortest path routing on the square, or even an approximate version of it, generates congested

areas on the center of the network. We have already discussed that this phenomenon is not desirable. The same problem is present on the rectangle, on the disk, and on any two dimensional convex deployment of the network, which is the common case in practice. Here, the idea is to relinquish shortest paths so as to get rid of congested areas, with the goal of improving security, energy efficiency, and tolerance to selfish behavior of the multi-hop wireless network. As the first step, we have to realize that there do exist metric spaces that do not present the problem. First, we need a formal definition of the key property of the metric space we are looking for.

**DEFINITION 1.** *Consider a multi-hop wireless network deployed on a space  $S$ . Fix a node  $u$  and choose its position on  $S$  arbitrarily. Then, deploy the other nodes of the network uniformly and independently at random. We will say that  $S$  is symmetric if, chosen two nodes  $v_1$  and  $v_2$  uniformly at random in the network, the probability that  $u$  is on the shortest path from  $v_1$  to  $v_2$  does not depend on its position.*

Clearly, the disk is not a symmetric space as in the above definition. It has been clearly shown in [17]—if node  $u$  is on the center of the circle or nearby, the probability that  $u$  is traversed by a message routed along the shortest path from a random source node  $v_1$  to a random destination  $v_2$  is larger than that of a node away from the center of the network area. Clearly, the square has exactly the same problem. This claim is confirmed by our experiments: 25% of the shortest paths traverse a relatively small central disk whose area is 3% of the entire square.

To solve these problems, our idea is to map the network nodes onto a symmetric space (the *outer space*) through a mapping that preserves the initial network properties (such as distribution, number of nodes, and, with some limitations, distances between them). Note that there is no need that the mapping be continuous (actually, restricting to continuous mappings would make our idea lose most of its interest). The second step is to route messages through the shortest paths as they are defined on the outer space. When the outer space and the corresponding mapping are clear from the context, we will call these paths the *outer space shortest paths*. Since the outer space is symmetric, we can actually prove that every node in the network has the same probability of being traversed by an outer space shortest path, on average. In the following section we will see that, based on this idea, we can design practical routing protocols that do not have highly congested areas, weaker security, and all the problems we have been discussing here. Furthermore, the routing protocol that we will present prolongs considerably the network lifetime. Now, let's make a step back and proceed formally.

Let  $S$  be the original space where the network is deployed, and let  $T$  be the outer space, an abstract space we use to describe routes, both metric spaces with respective distances  $d_S$  and  $d_T$ . We are looking for a mapping function  $\phi : S \mapsto T$  with the following properties:

1. if  $x$  is a point taken uniformly at random on  $S$ , then  $\phi(x)$  is also taken uniformly at random on  $T$ ;
2. for every  $r > 0$ , and every  $u, v \in T$ ,  $u \neq v$ , if  $d_T(\phi(u), \phi(v)) \leq r$  then  $d_S(u, v) \leq r$ .

Property 1 guarantees that a uniform traffic on  $S$  is still a uniform traffic when mapped onto  $T$  through  $\phi$ , and Property 2 says that paths on  $T$  are paths on  $S$ , when the nodes are mapped into  $T$  using  $\phi$ . Later we will see why these properties are important.

**DEFINITION 2.** *A mapping  $\phi : S \mapsto T$  is fair if it enjoys Properties 1 and 2.*

Once such a fair mapping has been fixed, any message from node  $u$  to node  $v$  can be routed following a shortest path between the images of  $u$  and  $v$  and through the images of some of the network nodes under  $\phi$  on space  $T$ . Let  $\phi(u), \phi(w_1), \phi(w_2), \dots, \phi(w_h), \phi(v)$  be such a path. Being  $\phi$  a fair mapping, the path  $u, w_1, w_2, \dots, w_h, v$  is a well defined path on  $S$ . Indeed, any two consecutive nodes in the shortest path on  $T$  are neighbors in  $S$  as well, thanks to Property 2. If  $T$  is *symmetric* as in Definition 1, the routing through  $\phi$  would be well distributed over  $T$ , since  $\phi$  has Property 1. Hence, this path can be used to route messages on  $S$ , giving as a result a homogeneous distribution of the message flow over all the original network area.

**THEOREM 1.** *Let  $\phi : S \mapsto T$  be a mapping from source metric space  $S$  to target metric space  $T$ . Assume that  $\phi$  is fair and  $T$  is symmetric. Fixed a node  $u \in S$ , deployed the other nodes of the network uniformly at random, and taken a source  $v_1 \in S$  and a destination  $v_2 \in S$  uniformly at random, the probability that the outer space shortest path from  $v_1$  to  $v_2$  defined by  $\phi$  traverses  $u$  is independent of the position of  $u$  on  $S$ .*

The above theorem shows how to build a routing protocol on a not symmetric network area, in such a way that the message flow is distributed homogeneously over all the network. What is needed is to determine a symmetric space (the outer space) and a fair mapping for it, and then to “transform” the shortest paths on the original network area into the corresponding outer space shortest paths.

We assume that the original network area is a square of side 1. An excellent candidate as a symmetric outer space is the torus. A torus is a 3-dimensional surface that we can model as  $T = [0, t] \times [0, t]$ . Let  $u_x$  and  $u_y$  be the coordinates of the position of node  $u$  on the torus. We can endow  $T$  with the following distance  $d_T$ :

$$d_T(u, v) = \sqrt{d_x^2 + d_y^2}, \quad (1)$$

where

$$d_x = \min\{|u_x - v_x|, t - |u_x - v_x|\}, \text{ and} \quad (2)$$

$$d_y = \min\{|u_y - v_y|, t - |u_y - v_y|\}. \quad (3)$$

The common way to visualize a torus is to consider a square, and then to fold it in such a way that the left side is glued together with the right side, and that the top side is glued together with the bottom side. In the following, we will picture the torus unfolded, just like a square, as it is commonly done to easily see this 3-dimensional surface as a 2-dimensional one.

**FACT 1.** *A torus surface is symmetric as in Definition 1.*

Clearly, virtually no wireless network in real life is deployed on a torus. Here, we are using the torus just as an abstract space. We are *not* making any unreasonable assumption on the nodes of the network being physically placed on a torus like area with continuous boundaries, nor are we assuming that the network area becomes suddenly a torus. Indeed, we assume that the real network is deployed on the square, where the nodes close to one side *cannot* communicate with the nodes close to the opposite side. Crucially, the paths used to deliver the messages are computed as they are defined through a fair mapping onto the torus, the outer space. Coming back to our idea, now that the target symmetric outer space has been chosen, what is left to do is to find a fair mapping  $\phi_{ST}$  from the square to the torus.

Let  $S = [0, 1] \times [0, 1]$  be a square, and let  $T = [0, 2] \times [0, 2]$  be a torus. We propose to define  $\phi_{ST}$  as follows:  $\phi_{ST}((x, y)) = (x', y')$

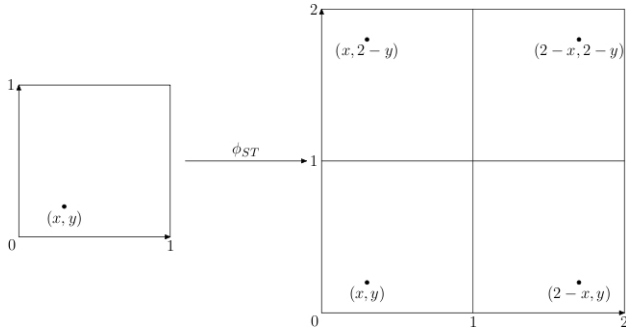


Figure 1: Example of mapping a point from the square to the torus through  $\phi_{ST}$ . Point  $(x, y)$  on the square  $S = [0, 1] \times [0, 1]$  has four possible and equally probable images on the torus  $T = [0, 2] \times [0, 2]$ . According to  $\phi_{ST}$ , only one of the images will actually appear on  $T$ .

where:

$$x' = \begin{cases} x & \text{with probability } 1/2, \\ 2-x & \text{with probability } 1/2, \end{cases}$$

and

$$y' = \begin{cases} y & \text{with probability } 1/2, \\ 2-y & \text{with probability } 1/2. \end{cases}$$

Even though  $\phi_{ST}$  is partly probabilistic, this does not mean that routing in outer space is a *random* routing scheme, like sending the packet along a Brownian path or like sending the packet to a random intermediate (an idea that has been used a lot in routing in parallel architectures and, later, also in network routing). Indeed, it is pretty easy to come up with a very similar completely deterministic version of  $\phi_{ST}$  with exactly the same properties, for our purposes. This deterministic version, however, is more complex to describe and to deal with, and this is the sole motivation to choose a partly probabilistic, and technically simpler, version.

An example of  $\phi_{ST}$  can be seen in Figure 1, where a node on the square is mapped to one of the four equally probable images on the torus.

**THEOREM 2.**  $\phi_{ST}$  is a fair mapping with probability one.

**PROOF.** The full proof is technical, without adding much to the understanding of this work. Therefore, for the sake of brevity, we omit it.  $\square$

It's interesting to note that even if two points are neighbors on square, they might not be neighbors on torus when mapped through  $\phi_{ST}$ . Generally speaking, it is impossible to build a mapping with both this property and Property 2, since the square and the torus are topologically different.

The outer space shortest path between two nodes may be different from the corresponding shortest path. Clearly, it can't be shorter by definition of shortest path on  $S$ . A natural question to ask is whether we can bound the stretch, that is, how much longer may the outer space shortest path be compared with the corresponding shortest path? Unfortunately, the answer is that the stretch cannot be bounded by a constant. However, quite surprisingly, we can prove a very good constant bound in the case when many messages are sent through the network, that is the common case in practice. Indeed, while in the worst case the stretch can be high, it is not

on average if we assume a uniform traffic. This claim is formalized in the following theorem, where we show that, on expectation, the distance of the images under  $\phi_{ST}$  of two nodes taken uniformly and independently at random is at most the double of the original distance.

**THEOREM 3.** If nodes  $u, v$  are taken uniformly at random on the square  $S = [0, 1] \times [0, 1]$ , and  $\phi_{ST}(u), \phi_{ST}(v)$  are their respective images under  $\phi_{ST}$  on the torus  $T = [0, 2] \times [0, 2]$ , then

$$E[d_T(\phi_{ST}(u), \phi_{ST}(v))] \leq 2E[d_S(u, v)].$$

**PROOF.** Let  $u, v \in S$  be two nodes whose position is taken uniformly at random, and let  $E[d_S(u, v)] = \mu$  be the expectation of their distance on  $S$ . Since  $\phi_{ST}$  is fair, also  $\phi_{ST}(u)$  and  $\phi_{ST}(v)$  are taken uniformly at random in the torus. Clearly, the distance between  $\phi_{ST}(u)$  and  $\phi_{ST}(v)$  on the torus cannot be larger of the distance of  $\phi_{ST}(u)$  and  $\phi_{ST}(v)$  on a square  $S' = [0, 2] \times [0, 2]$ . Indeed, every path on the torus is also a path on the square (the opposite is not true); and the average distance of two random points in a square of edge two is the double of the average distance of two random points in a square of edge one. Therefore,

$$\begin{aligned} E[d_T(\phi_{ST}(u), \phi_{ST}(v))] &\leq E[d_{S'}(\phi_{ST}(u), \phi_{ST}(v))] \\ &= 2E[d_S(u, v)] \\ &= 2\mu. \end{aligned}$$

$\square$

In the following, we will see with experiments that the actual average stretch is even smaller.

Of course, it is always possible to use the outer space shortest path only when the stretch of that particular path is small, and to use the classical shortest path when the stretch is high and the outer space shortest path is going to cost a lot more. However, we do not perform these kind of optimizations—even though they may reduce the global energy required by the network to deliver the messages, they also unbalance the load among the nodes. Therefore, we want to consider routing in outer space in its cleanest version. In the following, we will implement our idea in a practical routing protocol derived from geographical routing, and show its performance by means of experiments.

## 4. ROUTING IN OUTER SPACE IN PRACTICE

We start from geographic routing, a simple protocol that, when the network is dense enough, can be shown to approximate shortest path routing quite well [15]. Here, we define *outer space geographic routing*, its outer space counterpart.

In geographic routing, the destination of a message is a geographical position in the network area—in the square in our case. Every relay node performs a very simple protocol: Send the message to the node that is closer to destination. If such a node does not exist, then the message is delivered. If the network is dense, every message is delivered to the node closest to destination. It is known that this simple version of geographic routing sometimes is not able to deliver the message to the node closest to destination, and there are plenty of ways to overcome this problem in the literature. However, we do not consider these extensions (outer space geographic routing could as well be based on these more complex and complete versions), since the increased complexity do not add much to this work.

Outer space geographic routing works quite as simply. Every relay node looks at the destination  $x$  of the message, and forwards it to

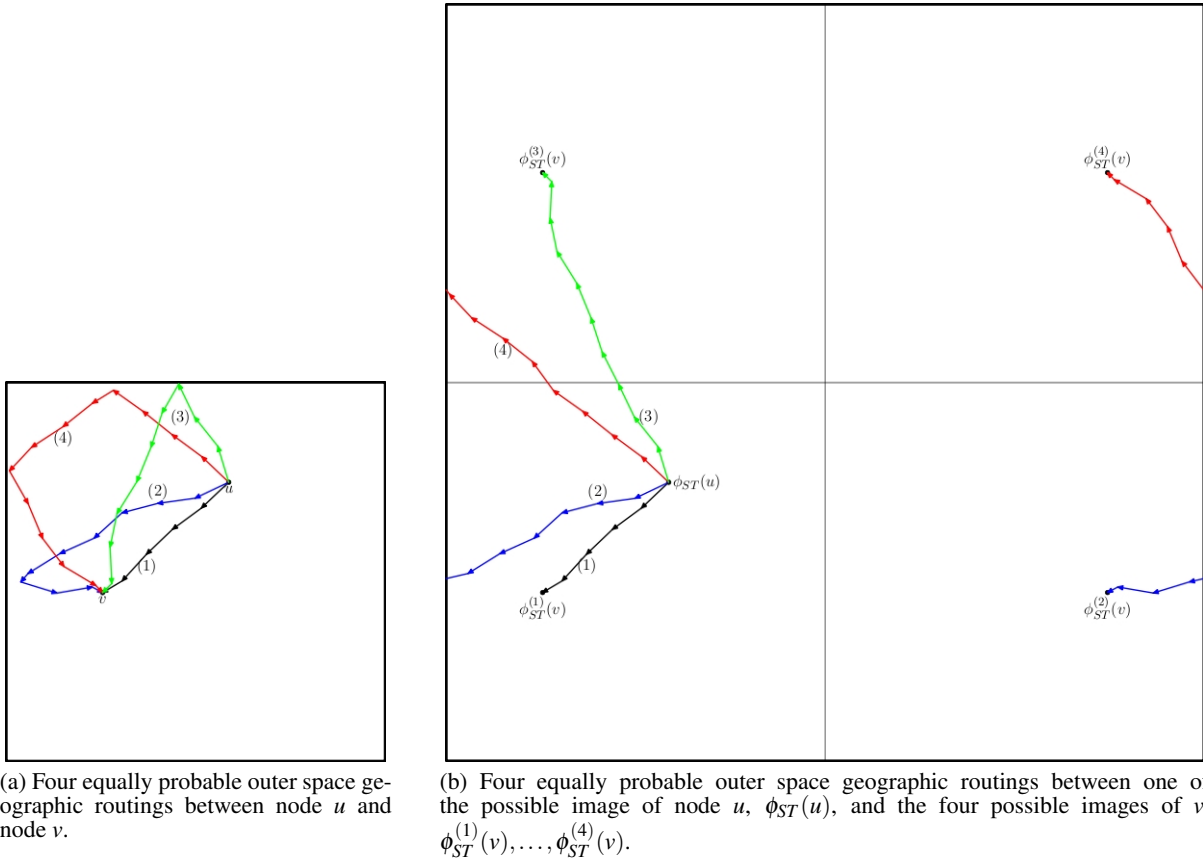


Figure 2: Assume, without loss of generality, that  $\phi_{ST}(u)$  is fixed. Subfigure (b) shows the four equiprobable shortest paths from  $\phi_{ST}(u)$  to the four possible  $\phi_{ST}(v)$ . Subfigure (a) shows the corresponding four equiprobable outer space shortest paths. Path (1) is just the traditional geographic routing between  $u$  and  $v$ . The network used to build this example is made of 6,441 nodes. (If you choose another image for  $\phi_{ST}(u)$ , the shortest paths are moved in the torus without changing the corresponding outer space shortest paths.)

the node  $u$  that minimizes  $d_T(\phi_{ST}(x), \phi_{ST}(u))$ . Just like geographic routing, implemented on the outer space.

Take, as an example, a message from node  $u$  destined to a geographic position close to node  $v$ . According to the definition of  $\phi_{ST}$ , each node on the square  $S$  has four possible and equally probable images on the torus  $T$ . This implies that for each pair  $u, v$  of nodes on  $S$  there are four possible and equally probable pairs of images  $\phi_{ST}(u), \phi_{ST}(v)$  on  $T$ . (Actually, there are 16 possible and equiprobable such couples, which fall into 4 different classes of symmetry up to isomorphism.) This yields four possible and different outer space geographic routes between the images  $u$  and  $v$  under  $\phi_{ST}$ . Hence, between any two nodes on the square there is one out of four different and equally probable outer space routes. To see an example of the four routes, see Figure 2.

To implement such a routing, it is enough that the nodes know their position in the square. Then, computing  $\phi_{ST}$  for itself and the neighbors is trivial and fast. Note that it is not really important that the nodes agree on which of the four possible images is actually chosen for any particular node (except for the destination, but the problem can easily be fixed). However, to get this agreement for every node it is enough to compute  $\phi_{ST}$  by using the same pseudo-random number generator, seeded with the id of the node being mapped.

#### 4.1 Node and Network Properties, Assumptions, and Simulation Environment

We model our network node as a sensor. A typical example can be the Mica2DOT node (outdoor range 150m, 3V coin cell battery). These nodes have been widely used in sensor network academic research and real testbeds. For our experiments, we have considered networks with up to 10,000 nodes, distributed using a Poisson process on a square of side 1,500m. In the following, we will assume for the sake of simplicity that the side of the square is 1, and that the node transmission range is 0.1.

We inject a *uniform traffic* in the network—every message has a random source and a random destination uniformly and independently chosen. This type of traffic distribution is highly used in network simulations, for example when the goal is to study network capacity limits, optimal routing, and security properties [8, 37, 11]. We assume that the nodes know their position on the network area. Therefore, they need to know both their absolute position, and their position within the square. The nodes can get the absolute position either in hardware, by using a GPS (Global Positioning System), or in software. There exist several techniques for location sensing like those based on proximity or triangulation using different types of signals like radio, infrared acoustic, etc. Based on these techniques, several location systems have been proposed in the literature like infrastructure-based localization systems [33, 24] and

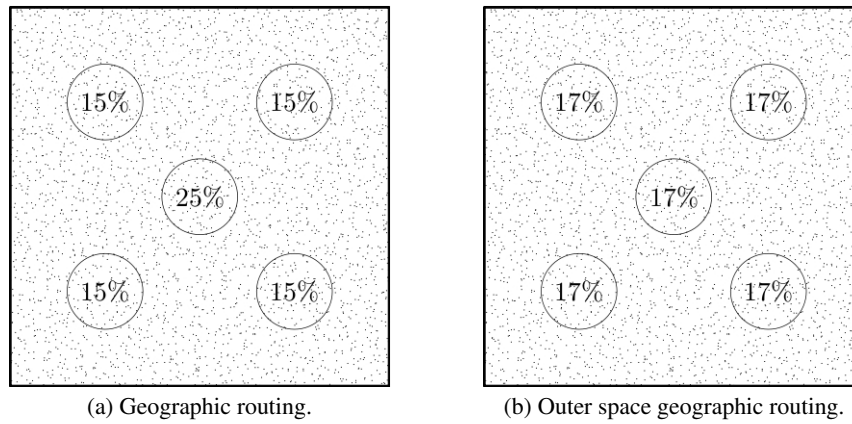


Figure 3: The average fraction of the messages whose routing path traverses the selected sub-areas of a network of 1,336 nodes, in the case of geographic routing and in the case of outer space geographic routing.

ad-hoc localization systems [5, 28]. In [10] you can find a survey on these systems while in [25] the authors present NoGeo: A location system that permits routing based on virtual positions of nodes.

Once the absolute position is known, we can get the nodes to know their relative position within the square by pre-loading the information on the deployment area, or by using one of the several techniques for boundary detection based on geometry methods, statistical methods, and topological methods (see [6, 16, 32]).

In the next two sections we present the results of the experiments we have performed, comparing our routing scheme with geographic routing over the same networks and with the same set of messages to route. For the experiments we have used our own event-based simulator. The assumptions and the network properties listed above have been exactly reflected in the behavior of the simulator.

## 4.2 Security-Related Experiments

In these experiments, we measure the number of messages whose routing path traverses five sub-areas of the same size in the network area. Every sub-area is a circle of radius 0.1 (incidentally, the same of the transmission radius of a network node), that corresponds to an area of 3.14% of the whole network surface. The sub-areas are centered in some “crucial” points of the network area: The center and the middle-half-diagonals points. The center of the network is known to be the most congested area. We want to test whether the middle-half-diagonal centered areas handle a significantly smaller number of messages. More specifically we consider the sub-areas centered in the points of coordinates  $(0.5, 0.5)$ ,  $(0.25, 0.25)$ ,  $(0.25, 0.75)$ ,  $(0.75, 0.25)$ ,  $(0.75, 0.75)$ , assuming a square of side one. Our experiments are done on networks with different number of nodes (from 1,000 to 10,000). For each network we have run both geographic routing and outer space geographic routing on message sets of different cardinality (from 50,000 to 1,000,000 messages, generated as an instance of uniform traffic). In Figure 3 we present the average of the results obtained with a network of 1,336 nodes generated by a Poisson process, but we stress that exactly the same results are obtained for networks with up to 10,000 nodes. As it can be seen, the experiments fully support the findings in [17]. Geographic routing (see Figure 3a) concentrates a relevant fraction of the messages on a small central area of the network, while the other sub-areas handle on average little more than the half. We have already dis-

cussed why this is dangerous, and important to avoid. Figure 3b shows the result with the same set of messages and the same network deployment, this time using outer space geographic routing. The message load in the central sub-area is 32% lower compared with the load of the same sub-area in the case of the geographic routing. Outer space geographic routing seems to transform the network area in a symmetric surface, making sure that the number of message handled by all the sub-areas remains reasonably low, 17%, and equally distributed. As a result, the load among the network nodes is equally balanced and there are no “over-loaded” areas. This network is intuitively stronger—there are no areas that are clearly more rewarding as objective of a malicious attack, and no areas that have more “responsibilities” than others.

Furthermore, Figure 3a clearly shows that, with geographic routing, it is not a good strategy to stay in the center of the network if you want to save your battery. If the nodes are selfish, it is a much better strategy to position in one of the sub-central areas, for example, where the battery is going to last 66% longer. Even better if you move towards one of the corners of the square, where there is virtually no traffic to relay. Conversely, when using outer space geographic routing, there is no advantage in choosing any particular position, since the relay traffic is equally distributed everywhere.

## 4.3 How to Live Longer by Consuming More Energy

In this section we present the experiments related to energy-efficiency. What Theorem 3 says in a sentence is that the paths used by outer space geographic routing are on average (at most) twice as long as the paths used by geographic routing. This should have an immediate consequence on energy consumption: Messages routed with outer space geographic routing should make the network nodes consume more energy, up to twice as much. And actually it is so. What it turns out with our experiments is that using routing in outer space the average path stretch is 1.34. Even though this translates into a 34% larger global energy consumption, we will see that, in addition to better security and absence of congested areas, the network has also excellent benefits from an energy-efficiency point of view when using routing in outer space. Figure 4 shows the global energy used by a network of 1,625 nodes, with both geographic routing and outerspace geographic routing. We have done more experiments with different network sizes, up to 10,000 nodes, and the result does not change.

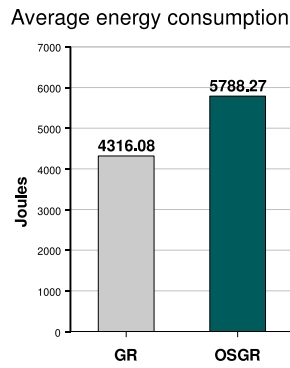


Figure 4: Global energy consumption of the network after running geographic routing (GR) and outer space geographic routing (OSGR) on sets of 50,000 messages each. The network is made of 1,625 nodes.

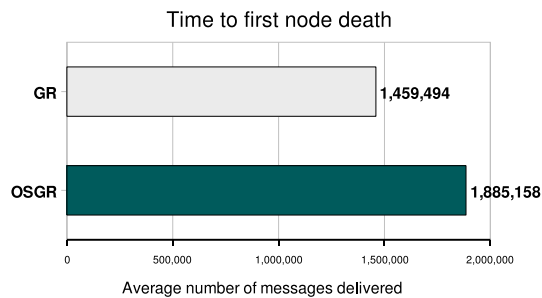


Figure 5: Time to first node death. The time is measured as the number of messages delivered to destination before the death of the first node. The network consists of 1,625 nodes. GR stands for geographic routing while OSGR stands for outer space geographic routing.

Usually, when a wireless network consumes more energy, its life is shorter. However, it is not always the case. Sometimes it is better to consume more energy, if this is done more equally in the network. This is exactly what happens with outer space geographic routing. We consider four measures of network longevity: time to first node death, time to loss of efficiency in message delivery, time to loss of network area coverage, and time to network disconnection. These measures are well-known, used in the literature [2, 3, 38], and collectively cover most of the concerns related to network lifetime. We have made four sets of experiments, each using one of the above ways to measure the longevity of the network. In each of the experiments we count the number of messages that are successfully delivered before network “death”, where network death is defined according to each of the above four measures. The first set of experiments is done according to the first measure. We have generated a network, a uniform traffic, and injected the traffic into two copies of the same network, one using geographic routing and one using outer space geographic routing. This has been iterated several times with networks of different sizes. The result is shown in Figure 5, where we show the number of messages delivered on average by a network of 1,625 nodes (the result does not change by considering network of different size), using both routing protocols.

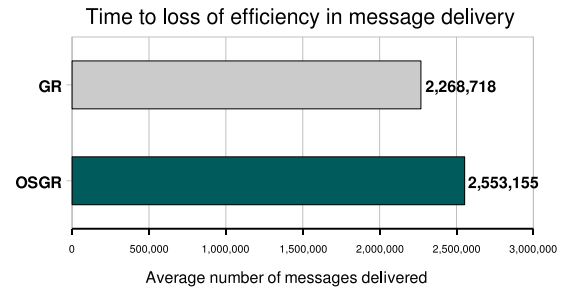


Figure 6: Time to loss of efficiency in message delivery. The time is measured as the number of messages delivered to destination before the delivery success ratio falls under 95%. The network considered is made of 1,625 nodes. GR stands for geographic routing while OSGR stands for outer space geographic routing.

As you can see, the network lifetime when using outer space geographic routing is 29.17% longer on average than geographic routing. As a matter of fact, the number of messages successfully delivered by the network until the very first node death is much larger with routing in outer space. Figure 6 shows the result we get when considering the second definition of network lifetime. In this case, we consider the network dead when it is not efficient any more in delivering messages. Note that geographic routing (and similarly its outer space version) has the problem of “dead ends”, places where the message cannot proceed because there is no node closer to destination, while the destination is still far. There are a number of solutions to this problem, and there do exist more sophisticated versions of geographic routing that know how to deliver a message whenever there is a path between source and destination. These solutions can be used both by geographic routing and by outer space geographic routing. However, when the network is not able any longer to deliver messages without these sophisticated add-ons, that means that the network is deteriorated. We use this as a measure of the quality of its structure. In this set of experiments we count the number of messages that reach destination until the success ratio of message delivery falls under some threshold (in our case 95%). As it can be seen in the figure, also in this case outer space geographic routing wins and prolongs the life of the network by 12.54% on average.

The third set of experiments is related to area coverage. One of the main application scenarios of sensor networks is the monitoring of some area of interest. In such applications, a must in terms of network properties is the fact that the area of interest has to be fully covered by the network sensing power. Of course, as long as the nodes begin to die, achieving this task becomes more and more difficult. We have performed our experiments assuming that sensing radius is 0.1, just like transmission radius. Again, outer space geographic routing is better and guarantees area coverage much longer. From Figure 7, you can see that routing in outer space increases network lifetime of 24,23% when considering coverage. Lastly, the fourth set of experiments consider network lifetime until network disconnection. Note that connectivity is one of the most important network properties, and that it is *different* from network coverage. Also in this case, outer space geographic routing wins over geographic routing. As it can be seen from Figure 8, with routing in outer space the network lives 20,42% longer, on average. Since security usually comes at a price, this is somewhat surprising. Routing in outer space delivers a network that, simulta-



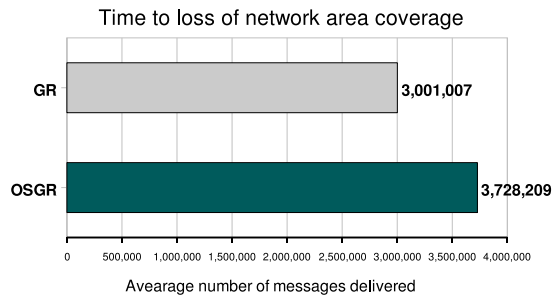


Figure 7: Time to loss of area coverage. The time is measured by the number of messages delivered to destination before the first loss of coverage of the sensing area. The network considered is made of 1625 nodes. GR is for Geographic Routing while OSGR is for Outer Space Geographic Routing.

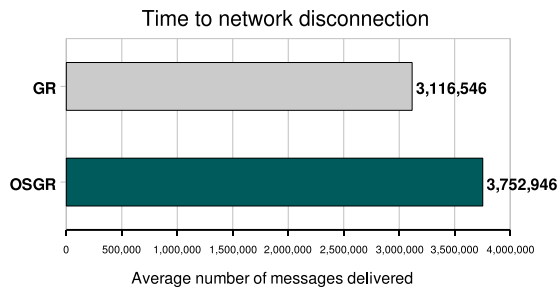


Figure 8: Time to network disconnection. The time is measured by the number of messages delivered to destination before network disconnection. The network considered is made of 1625 nodes. GR stands for geographic routing while OSGR stands for outer space geographic routing.

neously, offers less front for an attack and is more energy-efficient according to several different definitions of network lifetime.

## 5. CONCLUSIONS

Uniform traffic injected into multi-hop wireless networks generates congested areas. These areas carry a number of non-trivial issues about security, energy-efficiency, and tolerance to (a particular case of) selfish behavior. In this paper we describe routing in outer space, a mechanism to transform shortest path routing protocols into new protocols that do not have the above mentioned problems.

Routing in outer space guarantees that every node of the network is responsible for relaying the same number of messages, on expectation. We have shown that a network that uses routing in outer space does not have congested areas, does not have the associated security-related issues, does not encourage selfish positioning, and, in spite of using more energy globally, lives longer of the same network using the original routing protocol, according to a set of measures for network lifetime that collectively cover all the major concerns usually considered in the literature.

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